

## EXPLORING UNCERTAINTY IN FLOW UNIT IDENTIFICATION AND PERMEABILITY PREDICTION

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**Abstract:** The study proposes a comparative uncertainty analysis of the main methods for permeability prediction or estimation, including the Cluster analysis (K-means), the Kozeny-Carman (KyC) equation for flow unit identification, and the K-nearest neighbor Density Estimate (KNN) algorithm, Kozeny-Carman equation, and One Flow Unit (OFU) for permeability prediction or estimation. The proposed analysis is applied to 13 wells in the Sacha field located in the Amazon region of Ecuador, targeting the Hollin and Napo formations, which mainly consist of sandstone, limestone, and shale. The selected wells have a sufficient number of laboratory measurements of permeability and electrical logs of porosity, permeability, natural gamma ray, medium, and deep resistivity. Initially, the K-means clustering and KyC methods are applied to identify the flow units, followed by a regression process to calculate the permeability using the KNN, KyC, and OFU methods. During the clustering process, the KyC method yielded better results, with the experimental data exhibiting uncertainties of less than  $\pm 35$  mD, except in the outlier flow unit with an average porosity of  $16.86\% \pm 3.87\%$  (Flow Unit D) whose average permeability is 407.52 mD and uncertainty of  $\pm 504.10$  mD. For software simulation purposes, it is recommended to utilize the KyC method, as it employs basic concepts and equations in accordance with hydraulic principles.

**Keywords:** *uncertainty, permeability prediction, Sacha, flow units, K-nearest neighbor density estimate algorithm, cluster analysis.*

### 1. INTRODUCTION

The process of modeling an underground reservoir requires the permeability property determination, but this property can be measured by pressure test or directly by core samples (Remeczki et al. 2020, Fanchi 2018). This determination of the permeability is only developed in small portions of the reservoir. Therefore, the prediction process of the permeability is essential. The results obtained from permeability values vary widely between the laboratory data and the predictions of the different methods, however these predictions are used for modeling. Why are these values used in modeling despite their relatively wide difference? What is the method that

provides the best results? It is very important to know the uncertainties involved in each of the values of the methods used to predict permeability, since in this way the most appropriate method can be used.

The uncertainty in any measurement process has three components (Berg et al. 2021): the variation between the sample and the same rock type with heterogeneity, experimental uncertainty during the measurement, and the interpretation process related to the model application. Few research evaluates and gives directly the values of permeability (Johnston and Beeson 1944) or others evaluate the uncertainty of the relative permeability (Berg et al. 2021, Mathias et al. 2013) but not the sample data permeability.

Normally, laboratory measurements are not carried out in all wells and at all depths, so it is decided to use well logs to obtain permeability values and identify flow units through different processes. In some cases, the Kozeny-Carman equation is used to discretize the porosity values and based on a certain number of laboratory measurements of permeability, identify the flow units, and obtain the permeability by regression for the other zones and wells. For instance, (Belhouchet and Benzagouta 2019) use the Kozeny-Carman equation with the DRT (Discrete Rock Typing method) for predict the permeability in Algerian B-H oil field reservoir. This reservoir is composed of sandstone, limestone and dolomites and the results are based in the Correlation Coefficient R to determine if the estimation is right or wrong. However, they never expo the data of the permeability regression. Abbaszadeh et al. (1996), Amaefule et al. (1993) and Perez et al. (2005) use the same equations with different variations but with the main similar idea.

On the other side, Aminian et al. (2003) proposes the use of neural networks to base on training data predict the permeability and identify the flow units. It is similar to using the K-nearest-neighbor Density Estimate (KNN) which needs training data. In the case of study of the Norcan East Field (Bhattacharya et al. 2008) the methodology offers a complete process which includes validation based on the water saturation and capillary pressure which appear in the transition's zones. This methodology is more complete but never calculates the uncertainty of the permeability values. Data from 13 wells were used in this research, which are in total 428 samples measured its porosity and permeability. Three methods are proposed to identify the flow units, one based in the size of porous that we call Kozeny-Carman (KyC) method, other is the cluster analysis algorithm called K-means which identified centroids and classified the data according to the nearest points (Szabó et al. (2019), Ali, Sheng-Chang (2020)). In addition to, on this research the called One Flow Unit (OFU) method which as its name implies all the data belongs to one flow unit, it is because in the process of modeling it is always used and certainly sometimes It gets the best history match with the real fluid production (Krause et al. 2009).

Permeability was estimated using the Kozeny-Carman equations with DRT (Discrete Rock Typing) (Belhouchet and Benzagouta 2019, Amaefule et al. 1993) but also uses the K-nearest-neighbor Density Estimate (KNN) method (Gómez et al. 2022) which is based on a test data for learning and estimate the permeability. The third method uses exponential matching in One Flow Unit (OFU).

In addition, the uncertainty for the real sample data is determined with Equations (14), (15) and (16). And for the estimation of the permeability the equation used will be determined with exponential matching (Papadopoulos and Yeung 2001). However, the calculation of the error develops using the Equation (17). The results show that the error and the uncertainty do not have any similarity and the uncertainty is always present.

## 2. METHODOLOGY

Permeability and porosity data are measured on 428 samples obtained from 13 wells in the Sacha field located in northeastern Ecuador (Baby et al. 2014). This data was matched with the well logs of natural gamma ray, superficial, intermediate, and deep resistivity, neutron porosity, gamma-gamma density and spontaneous potential. The methodology is divided into three stages:

- Flow unit identification,
- Permeability estimation,
- Uncertainty and error of permeability determination.

### 2.1. Flow Unit Identification

Using the Kozeny-Carman methodology four flow units were identified: A, B, C and D. The equations used are (Amaefule et al. 1993):

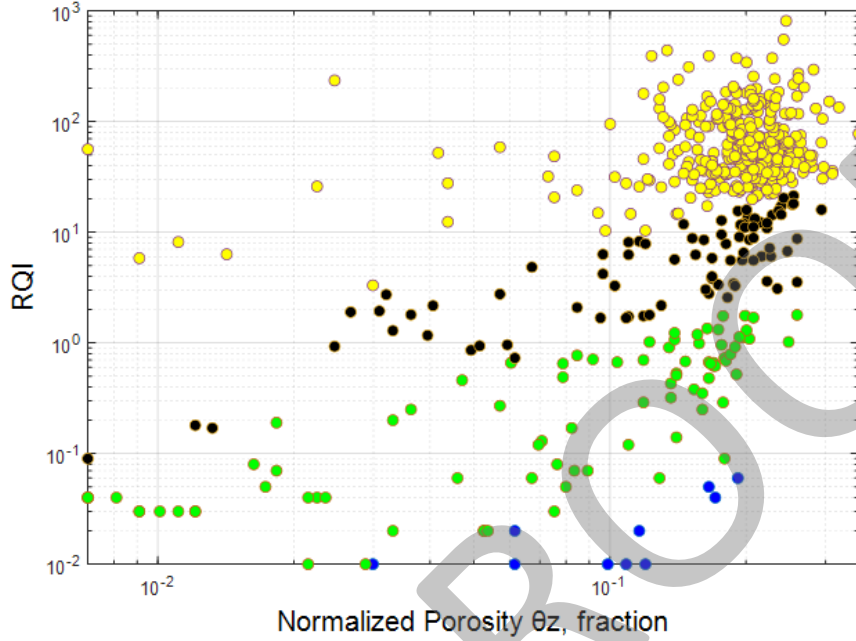
$$\theta_z = \frac{\theta}{1 - \theta} \quad (1)$$

$$RQI = 0.0314 \frac{K}{\theta} \quad (2)$$

$$FZI = \frac{RQI}{\theta_z} \quad (3)$$

$$DRT = 2 \text{Log}_e FZI + C \quad (4)$$

where  $\theta_z$  is normalized porosity in volume fraction, RQI is Rock quality index, K is permeability in mD,  $\theta$  is porosity in volume fraction, FZI is Flow zone indicator, DRT is Discrete rock typing. According to the theory in a graphic Log RQI vs Log  $\theta_z$  must draw parallels lines to differentiate the flow units (see Figure 1).



**Figure 1**

*Log RQI vs log  $\theta_z$  of 428 samples of the Sacha Field. Blue, green, black and yellow represent the corresponding flow units A, B, C, D identified*

Discrete rock typing (DRT) gives integer numbers, in this case ranging from 6 to 27, and they are organized into larger groups called flow units. In this case, using MATLAB, the grouping of the values was easier because the parallel lines in Figure 1 must have the same slope and the numbers are in order. In Table 1 are the numbers that are related to the flow units A, B, C, D.

The other method used to identify the flow units was using the Cluster Analysis methodology. K-means cluster analysis is a simple unsupervised statistical method that orders the objects of a multivariate dataset into groups (flow units) using the information of similarities given by metric distance (see Figure 2). The method is sensitive to the scale difference between variables, so normalization of the data set is required. Then, each object is designated into a non-overlapping group of great homogeneity and large differences from other groups. For further explanation see Szabó et al. (2019) and Ali and Sheng-Chang (2020). Mathematically, the method is expressed by the following equation:

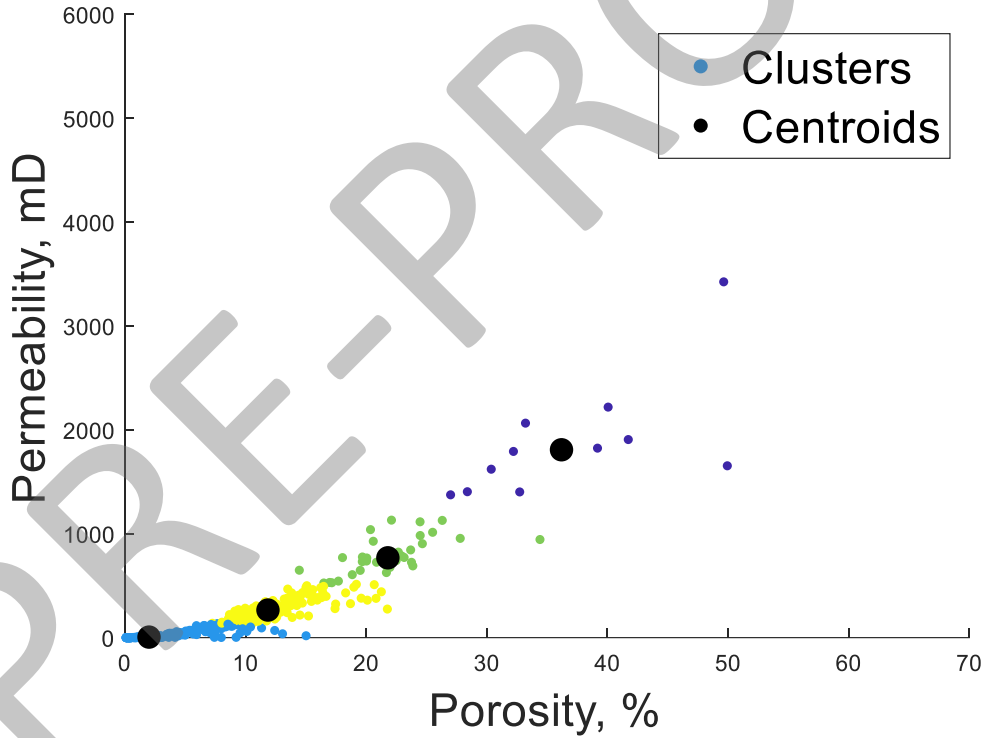
$$J = \sum_{j=1}^k \sum_{i=1}^n \|x_i^{(j)} - c_j\|^2 \quad (5)$$

where  $J$  is objective function,  $x_i$  is the  $i$ -th analyzed object,  $i= 1, \dots, n$ ,  $c_j$  is the  $j$ -th cluster centroid,  $j= 1, \dots, k$ ,  $K$  is optimal number of clusters. The objective function converges at the minimum sums of square deviation of objects  $x_i$ , from the cluster centroid  $c_j$ .

The ‘‘City Block’’ distance metric is incorporated for this study. Here, each cluster centroid is the component-wise median of the points in the cluster

$$D_1 = \sum_{k=1}^N |x_k^{(i)} - x_k^{(j)}| \quad (6)$$

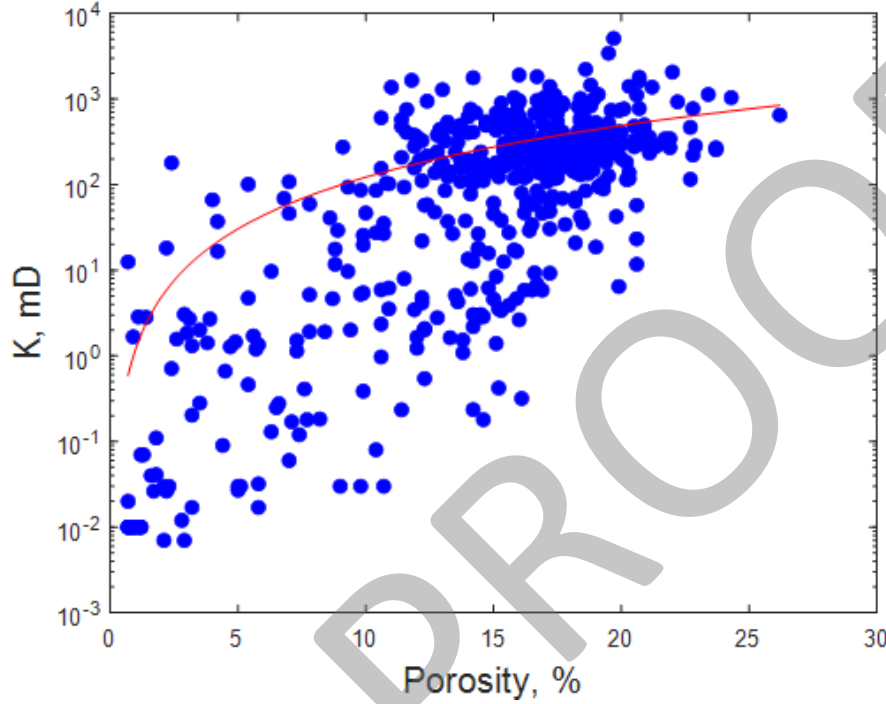
where  $D$  is sum of lengths between points,  $x_k^{(i)}$  is distance of  $x_k$  from the centroid in component  $i$ ,  $x_k^{(j)}$  is distance of  $x_k$  from the centroid in component  $j$ . In this case, the four flow units identified were named 1, 2, 3 and 4. The data classification can be seen on Figure 2:



**Figure 2**

*Permeability and porosity of 428 samples classified by K-means clustering algorithm. Light blue, yellow, green, and purple are the flow units 1, 2, 3, and 4 respectively. Black points are the centroids*

Finally, the One Flow Unit (OFU) method to complete permeability data is presented in Figure 3.



**Figure 3**

*Logarithm of permeability vs. porosity (%) of the 428 samples. Red line represents the exponential regression to predict the permeability*

## 2.2. Permeability estimation

The permeability was estimated first using an exponential regression for each flow unit A, B, C and D. The empirical equations are given below

$$K_A = 4.804 * 10^{-6} \theta^{3.994} \quad (7)$$

$$K_B = 0.00179 \theta^{2.862} \quad (8)$$

$$K_C = 0.01604 \theta^{2.849} \quad (9)$$

$$K_D = 1.521 \theta^{1.959} \quad (10)$$

The second method used for estimating the permeability was the K-nearest neighbor density estimate (KNN) which is a non-parametric method of estimating a probability density function. The algorithm estimates a function that predicts the rock

type(z) according to the log-well registered values. Every interpreted rock category x is a p-dimensional random variable X. This means the interpretation of the rock permeability will depend on the pre-established rock type z. The d(x,z) represents the Euclidean distance between x and z. X is an example of z, consequently x is the permeability measured and matched with the logs before the prediction (Hu et al. 2008, Mitra et al. 2002). The hypersphere of radius r about z is designated by Equation 11

$$A_{r,z} = \{X \mid d(x,z) \leq r\} \quad (11)$$

where  $A_{r,z}$  is volume of the hypersphere, r is radius of the hypersphere, x is a categorical class, and X is a variable with p dimensions. Then Equation 12 defines the density function:

$$f_N(z) = \frac{k(N)}{N} * \frac{1}{A_{rk(N),z}} \quad (12)$$

where  $f_N(z)$  is a function f to estimate z with N, k(N) is a sequence of positive integers from  $x_1$  to  $x_N$ , x is a rock type interpreted in a set of data. By the other hand, the OFU method determine the exponential equation. See Figure 3:

$$K_T = 0.9733\theta^{2.825} \quad (13)$$

### 2.3. Uncertainty and error of permeability determination

Here, the real sample data was measured in poropermeameter equipment whose precision is 0.1% for the porosity and 0.01 mD for the permeability. The process of divide the permeability in flow units suppose that in the modeling process the same equation will be used for all the data that belongs to this flow unit. It is similar to the up-scaling where a group of data of wells is assigned to a cell of a grid. For this reason, the Equation 14 is used for determining the uncertainty in the experimental data. The Equation 15 is used to determine the uncertainty when a regression process is developed. The Equation 16 is the porosity uncertainty necessary for the calculation of the permeability uncertainty (JCGM member organizations 2008)

$$u(k) = \sqrt{P_K^2 + S_K^2} \quad (14)$$

$$u(k) = \frac{\partial K}{\partial \theta} u(\theta) \quad (15)$$

$$u(\theta) = \sqrt{P_\theta^2 + S_\theta^2} \quad (16)$$

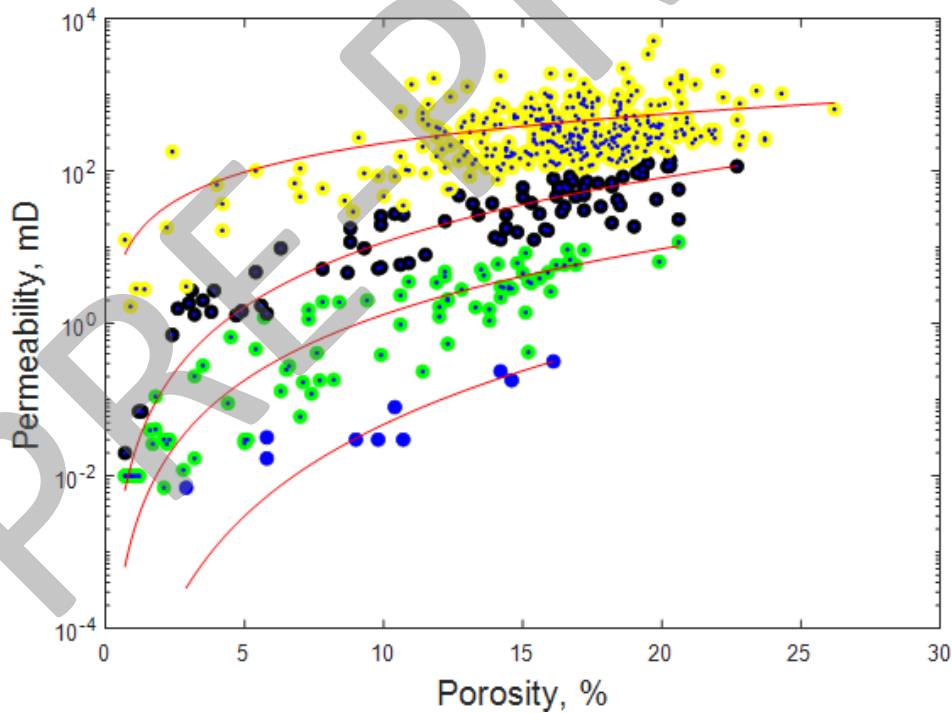
where  $u$  is the uncertainty of the permeability and porosity,  $P$  is a precision of the poropermeameter equipment for permeability and porosity,  $S$  is the Standard Deviation for porosity and permeability. The calculation of the error was also developed using the equation:

$$\%E = \frac{RV - EV}{RV} * 100 \quad (17)$$

where  $\%E$  is the data estimation Error with respect to the sample measured,  $RV$  is the real value with refer to the sample measured, and  $EV$  is the estimated value with the different proposed methods.

### 3. RESULTS

The results of the flow units and the permeability estimation according the KyC methodology is presented on the Figure 4, Table 1 and Table 2. The  $\theta_{\text{mean}}$  is the mean porosity in the flow unit,  $k_{\text{corr}}$  is the measured permeability,  $K_{\text{NN}}$  is the permeability estimated using the KNN method,  $E_{\text{KNN}}$  is the error between the measured and the estimated permeability,  $K_{\text{KyC}}$  is the permeability in the flow unit and  $E_{\text{KyC}}$  is the error. In the calculation of the errors the equation used was Equation 17.



**Figure 4**

*Logarithm of permeability vs. porosity (%) of the 428 samples divided in four flow units. Red lines represent the exponential regression to predict the permeability*



**Table 1**

Flow units A, B, C, and D determined using the KyC method with the DRT (discrete rock typing) with porosity ( $\Theta_{mean}$ ), permeability ( $k_{corr}$ ) measured in laboratory, and permeability calculated with KNN ( $K_{NN}$ ) and KyC ( $K_{KyC}$ )

DRT	FLOW UNIT	NUMBER ELEMENTS	$\Theta_{mean}$ %	$k_{corr}$ mD	$K_{NN}$ mD	E_KNN	$K_{KyC}$ mD	E_KyC
6	A	3.00	9.83	0.03	0.03	0.00%	0.07	131.88%
7		2.00	8.10	0.05	0.05	0.00%	0.05	4.28%
8		5.00	10.72	0.15	0.15	0.00%	0.28	81.82%
9	B	8.00	6.70	0.10	0.10	0.00%	1.36	1220.58%
10		5.00	6.56	0.13	0.13	0.00%	0.58	356.38%
11		5.00	9.50	0.46	0.46	0.00%	2.18	377.81%
12		13.00	7.27	0.60	0.60	0.00%	1.79	198.15%
13		19.00	10.35	2.04	2.04	0.00%	4.44	117.34%
14		21.00	9.50	2.88	2.88	0.00%	4.15	43.97%
15		15.00	10.81	4.28	4.28	0.00%	3.67	14.29%
16	C	21.00	10.41	8.42	8.42	0.03%	38.74	360.08%
17		11.00	14.59	23.46	19.83	15.46%	69.42	195.93%
18		16.00	13.09	30.12	30.12	0.00%	58.20	93.23%
19		33.00	14.78	62.62	62.62	0.00%	79.05	26.25%
20	D	41.00	16.95	142.72	141.69	0.72%	616.22	331.77%
21		79.00	17.69	230.72	227.98	1.19%	647.59	180.68%
22		66.00	16.91	327.78	327.78	0.00%	585.22	78.54%
23		29.00	16.39	551.21	545.49	1.04%	588.57	6.78%
24		26.00	15.07	770.47	770.47	0.00%	514.63	33.21%
25		6.00	14.85	1412.19	1412.19	0.00%	525.87	62.76%
26		2.00	17.75	2665.86	2665.86	0.00%	636.04	76.14%
27		2.00	15.75	3377.07	3377.07	0.00%	523.76	84.49%

In Table 2  $u_{R\Theta}$  is the porosity uncertainty in % determined using Equation 16,  $u_{RK}$  is the uncertainty in the permeability determined using Equation 14 with the  $S_k$  of each flow unit of KyC,  $u_{KNN}$  is the uncertainty in the KNN permeability determined with Equation 14 and the  $u_{R\Theta}$  for each KyC flow unit,  $U_{CK}$  is the uncertainty in the KyC permeability determined with Equation 15 and  $u_{R\Theta}$  for each KyC flow unit.

**Table 2**

Uncertainty and Error values in the KyC method for flow units ( $u_{R\Theta}$  Equation 16,  $u_{RK}$  Equation 14,  $U_{KNN}$  Equation 14,  $u_{CK}$  Equation 15 and 16) in KNN and KyC methods for permeability estimation

FLOW UNIT	# SAMPLES	$\Theta_{mean}$ %	$u_{R\Theta}$ %	$K_R$ mD	$u_{RK}$ mD	KNN_mD	$U_{KNN}$ mD	E_KNN	$K_{kyC\_mD}$	$u_{CK}$ mD	E_KC
A	10	9.93	±4.26	0.10	±0.11	0.10	±0.15	0.00%	0.17	±0.08	77.81%
B	86	9.15	±5.65	2.04	±2.56	2.04	±2.56	0.00%	3.19	±1.78	56.77%
C	81	13.29	±5.66	36.83	±34.74	36.34	±34.94	1.34%	63.17	±30.90	71.54%
D	251	16.86	±3.87	407.52	±504.10	405.83	±504.68	0.42%	601.49	±173.21	47.60%

Table 3 presents the flow units according the K-means clustering method:  $u_{R\theta}$  is the porosity uncertainty in % determined using Equation 16,  $u_{RK}$  is the uncertainty in the permeability determined using Equation 14 with the  $S_k$  of each flow unit of K-means,  $u_{KNN}$  is the uncertainty in the KNN permeability determined with Equation 14 and the  $u_{R\theta}$  for each K-means flow unit,  $U_{KyC}$  is the uncertainty in the KyC permeability determined with Equation 15 and  $u_{R\theta}$  for each K-means flow unit.

**Table 3**

*Uncertainty and error values in the K-means clustering method for flow units ( $u_{R\theta}$  Equation 16,  $U_{RK}$  Equation 14,  $U_{KNN}$  Equation 14,  $U_{KyC}$  Equation 15 and 16) in KNN and KyC methods for permeability estimation*

FLOW UNIT	# SAMPLES	$\Theta_{mean}$ %	$u_{R\theta}$ %	$K_R$ mD	$U_{RK}$ mD	$KNN\_mD$	$U_{KNN}$ mD	EKN N	$K_{kyC}$ Md	$U_{KyC}$ mD	EKyC
	173	14.98	±4.98	233.03	±514.99	231.55	±515.26	0.64 %	368.43	±38.31	58.10 %
	79	13.00	±6.57	199.37	±270.59	198.83	±270.69	0.27 %	287.29	±31.07	44.10 %
	134	15.20	±4.93	254.43	±341.91	254.43	±341.91	0.00 %	396.75	±59.86	55.94 %
	42	12.80	±7.16	364.01	±535.80	360.05	±535.90	0.01	399.22	±435.10	9.67%

In Table 4 we present the uncertainty and error with One Flow Unit method.

**Table 4**

*Uncertainty and Error values in the OFU method for permeability estimation*

K_OFU mD	$u_{UFO}$ mD	E_KOFU
438.70	±349.59	78.73%

#### 4. DISCUSSION

Unquestionably in this case, the KNN method gives the best result taking account the %Error (E\_KNN) (Table 1 and 2) for both grouping methods, it attributes because KNN uses test data for estimate the permeability. If the permeability property is needed the KNN is the best option. However, it recommends using KyC method in modeling process. For modeling the up scaling Fanchi (2018) means grouping permeability for assign values or equations to a complete cell or cells. In his publication, Wang (2018) arrives at a similar conclusion regarding the identification of flow units for lithological purposes. In this work, Wang writes, “KNN (K-Nearest Neighbors) clustering in machine learning is a very efficient clustering method applied in lithology identification, reservoir type recognition, flow unit classification, and so on. However, it is not consistently effective due to its inherent limitations, such as its initial center selection and clustering center shift caused by outliers.” Wang states that while the KNN method is generally efficient, it encounters problems with clustering, which he attributes to issues with the initial selection center (Wang et al. 2018). In the publication by Silva (2019) titled Petrofacies

Classification using Machine Learning Algorithms, the precision for predicting petrofacies using KNN is 92% for homogeneous layers, while for heterogeneous layers, it is reduced to 85%. In this research, they utilize an 80/20 split, meaning 20% of the data is used for testing, and 80% is for evaluation. The challenge in petrofacies identification lies in classifying heterogeneous layers. Permeability is a crucial aspect of petrofacies. This confirms the assertion because the data grouping directly addresses the heterogeneity of layers (Silva et al. 2020).

In this investigation % Error is calculated by comparing the measured data with the estimated data, and it is an individual comparison between two values, while the uncertainty first depends on the precision of measuring equipment and after of the clustering process. The standard deviation is an important part of the determination of uncertainty.

In the application of the KyC for identifying flow units, the suitable value of porosity varies from  $9.15 \pm 5.65$  % to  $16.86 \pm 3.87$  %. While the experimental data of permeability has a suitable value from  $0.1 \pm 0.11$  mD to  $407.52 \pm 504.10$  mD. Like, the estimated permeability varies from  $0.10 \pm 0.15$  mD to  $405.83 \pm 504.68$  mD with the KNN method. Comparable, in the KyC method the permeability varies from  $0.17 \pm 0.08$  mD to  $601.49 \pm 173.21$  mD. Certainly, the permeability has a huge uncertainty, and it increases when is tried to estimate with different methods.

By the other hand, in the application of the K-means method for identify flow units the suitable value of porosity varies from  $12.80 \pm 7.16$  % to  $15.20 \pm 4.93$ %. While the experimental data of permeability has a suitable value from  $199.37 \pm 270.59$  mD to  $364.01 \pm 535.80$  mD. Like, the estimated permeability varies from  $198.83 \pm 270.69$  mD to  $360.05 \pm 535.90$  mD with the KNN method. Comparable, in the KyC method the permeability varies from  $287.29 \pm 31.07$  mD to  $399.22 \pm 435.10$  mD. Here, the uncertainty is less in the KyC method than the KNN method. However, the % Error is higher for every mean permeability. Consequently, the KNN is better in individual analysis but in grouped data the KNN has higher uncertainty.

In the application of the OFU method for identifying flow units the suitable value of permeability is  $438.70 \pm 349.59$  mD with an error of 78.73%. If we compare this value with the other methods this value still inside the limits of the permeability measured or estimated for them. It means that the use of one flow unit in modeling is not a bad option considering that the uncertainty of permeability with the other methods has a huge variation.

## 5. CONCLUSIONS

According to our study, the best method to use in modeling process is KyC for flow units identification and permeability estimation. The uncertainty in Table 2 and 3,  $u_{KNN}$  (uncertainty in KNN method) and  $u_{CK}$  (uncertainty in method KyC) show smaller values in KyC method. The best method for determining the permeability is the KNN because the error is almost zero in all the flow unit classifications.

The flow unit D has uncertainty higher than the estimated value except in the KyC method, it is because the D flow unit is the one with bigger porous size and

permeability measures. The KyC method always uses the size of the porous to grouping the data.

The KyC method uses the size of the porous-like base for dividing the data while K-means uses only mathematics for dividing. However, using K-means is disquieting to clustering the data of natural gamma ray or resistivity logs to identify some match with the groups of permeability with porosity. If a good correlation is found, is possible to develop equations for predicting permeability with log data. Certainly, it is recommended to use K-means in K vs. natural gamma ray or K vs. Resistivity or K vs. density and compare with K-means of K vs. porosity.

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